

Hierarchical Power System Control using Fast Inverter-Based Resources

Prof. John W. Simpson-Porco

<https://www.control.utoronto.ca/~jwsimpson/>



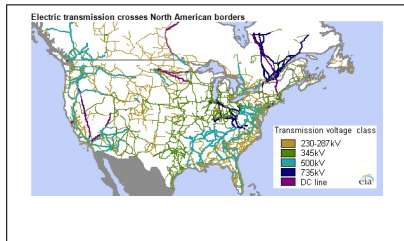
The Edward S. Rogers Sr. Department
of Electrical & Computer Engineering
UNIVERSITY OF TORONTO

PowerWeb Conference Keynote Talk

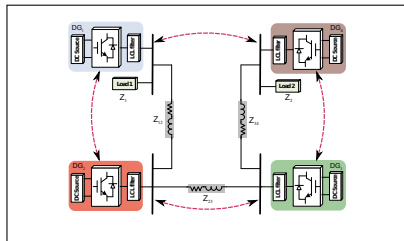
TU Delft, The Netherlands, September 27th, 2023.

Research in Power System Control and Optimization

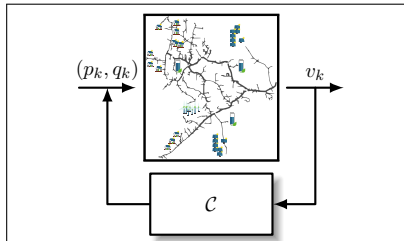
Power Flow Analysis & Algorithms



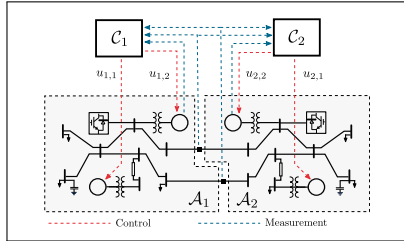
Microgrid Control & Optimization



Renewable Energy Integration



Next-Generation Hierarchical Control



Motivation for Advanced Grid Controls

Relevant Challenges:

- 1 RES integration \implies decreased inertia and control response
- 2 slow legacy monitoring/control architectures (e.g., SCADA)

(Some) Desirable Advances:

- 1 use of high-bandwidth **closed-loops** (e.g. 10+ samples/sec)
- 2 use of fast **inverter-based resources** (IBRs) for control
- 3 **hierarchical architectures** for (i) integration of many devices, (ii) situational awareness, (iii) low-latency localized response

▶ EPRI Whitepaper: *"Next-Generation Grid Monitoring and Control: Toward a Decentralized Hierarchical Control Paradigm"*

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Enabling Fast Control via Inverter-Based Resources

in other words, how do we make the modern grid more boring?

Big Picture: leverage fast actuators for fast control

1 Design Objectives

- **Fast** and **localized** compensation of disturbances
- Hierarchical/decentralized architecture (min. delay, **scalability**)
- Maintain real-time **operating constraints**

2 Design Constraints

- Premium on **simplicity** in design and implementation
- Integrable with **legacy controls**
- Use **realistically available** model information

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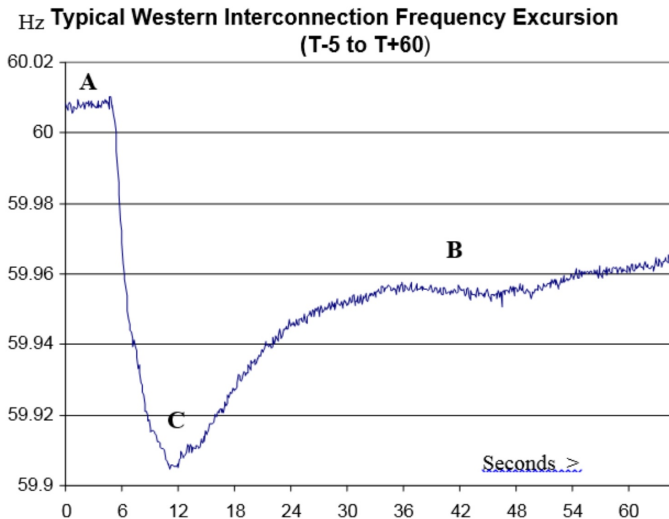
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Outline of Talk

- ① Fast Frequency Control via IBRs
- ② Fast Voltage Control via IBRs (maybe)
- ③ Hierarchical Transmission/Distribution Coordination
- ④ Parting Thoughts

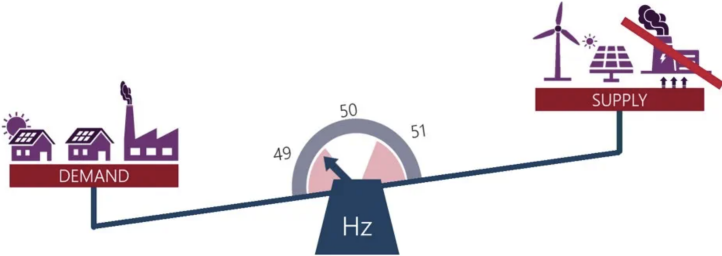
Primer on Traditional Frequency Control

Figure: NERC *Balancing and Frequency Control*



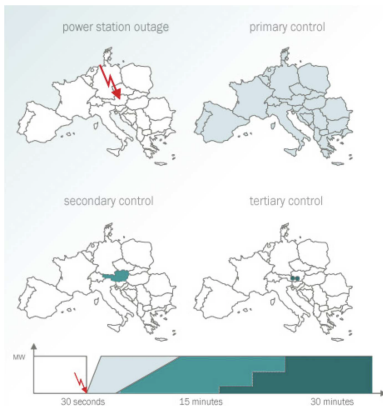
Frequency Control is Supply-Demand Balancing

Figure: AEMO

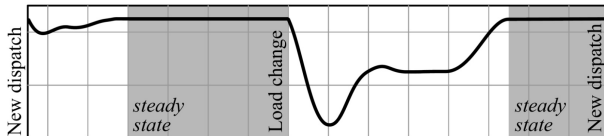


Stages of Power System Frequency Control

Figures: ENTSO-E, S. Dhople



- **Primary Control:** generators *everywhere* respond to help stabilize the frequency
- **Secondary Control:** rebalances the system so that every area achieves supply-demand balance
- **Tertiary Control:** Re-optimizes all generation minimize cost



Diagnosing The Patient

- Legacy frequency regulation is **slow**, because
 - (i) Turbine-governor systems on large generators are slow
 - (ii) The priority (correctly) is *robustness* not *performance*
 - (iii) High-inertia grids don't need fast rebalancing, so why bother
- Primary control essential, but provides limited localized response
- Regulation loop (LFC) is based on Cohn's frequency-biased net-interchange (ACE); this **ignores grid dynamics**

How should we re-think frequency control for low-inertia systems with fast actuators?

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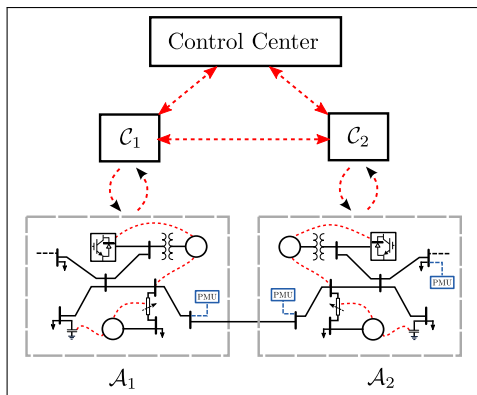
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Overview of Proposed Frequency Controller



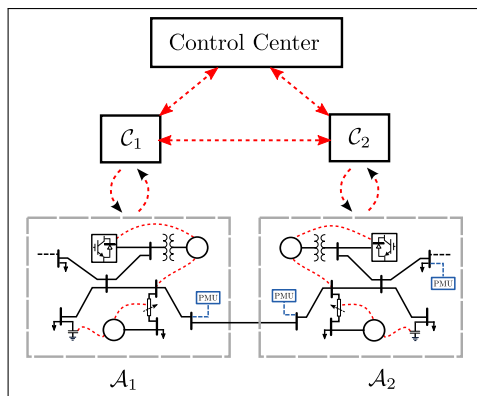
Bulk grid divided into small **local control areas** $\mathcal{A}_1, \dots, \mathcal{A}_N$ (e.g., a few substations each)

Measurements and resources locally available within each LCA

- 1 **Stage 1:** LCA-decentralized controllers C_k redispatch local IBRs
- 2 **Stage 2:** Centralized coordination for severe contingencies

Conceptual goal: very fast and localized secondary-like response

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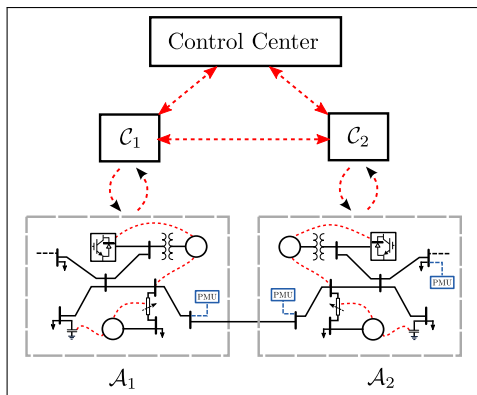
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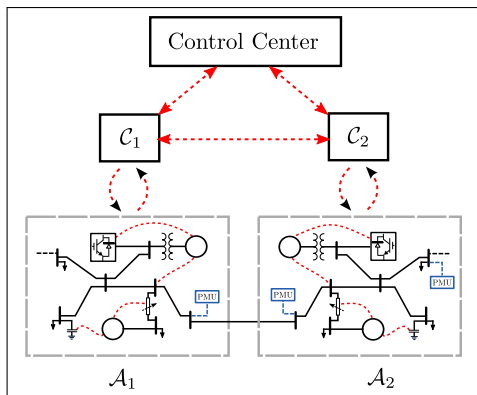
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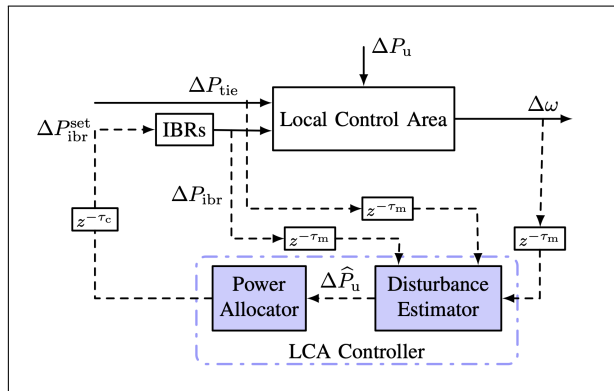
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Stage 1: Local Control Area (LCA) Frequency Control

Philosophy: quickly estimate and compensate all local imbalance

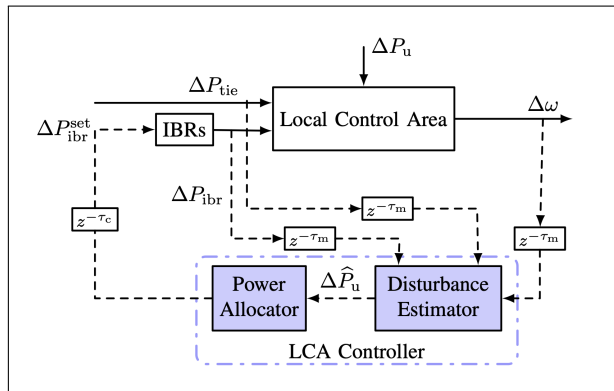


IBRs: can have local f/P droop curve, but must **accept a provided set-point**

- 1 **Disturbance Estimator**: real-time estimate of gen.-load mismatch
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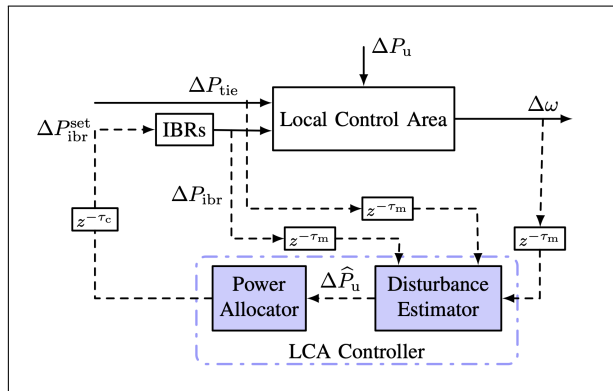


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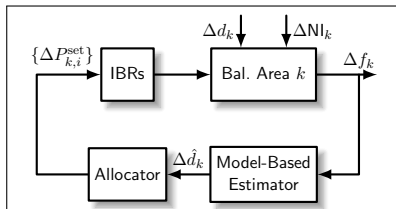


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Model-Based Fast Frequency Control

E. Ekomwenrenren et al., "Hierarchical Coordinated Fast Frequency Control ...," in IEEE TPWRS, 2021.



- IBRs have local droop curve

$$T_{k,i} \Delta \dot{P}_{k,i} = -\Delta P_{k,i} - \frac{\Delta f_{k,i}}{R_{k,i}} + \Delta P_{k,i}^{\text{set}}$$

- Inverter controls ensure $T_{k,i}$ is small (e.g., 200ms)

- **Identify** a simple dynamic model for each area + IBR dynamics

$$\Delta \dot{x}_k = A_k \Delta x_k + B_k (\Delta P_k^{\text{set}} - \Delta d_k + \Delta NI_k), \quad \Delta f_k = C \Delta x_k$$

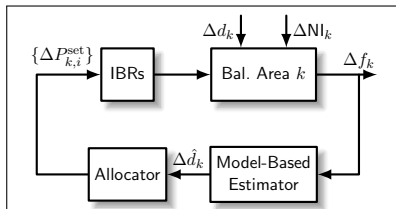
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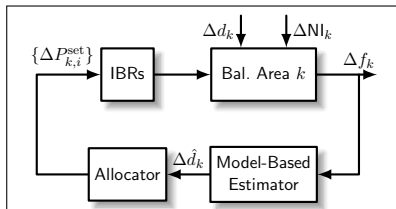
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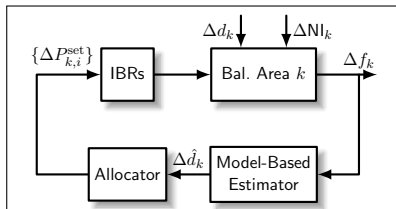
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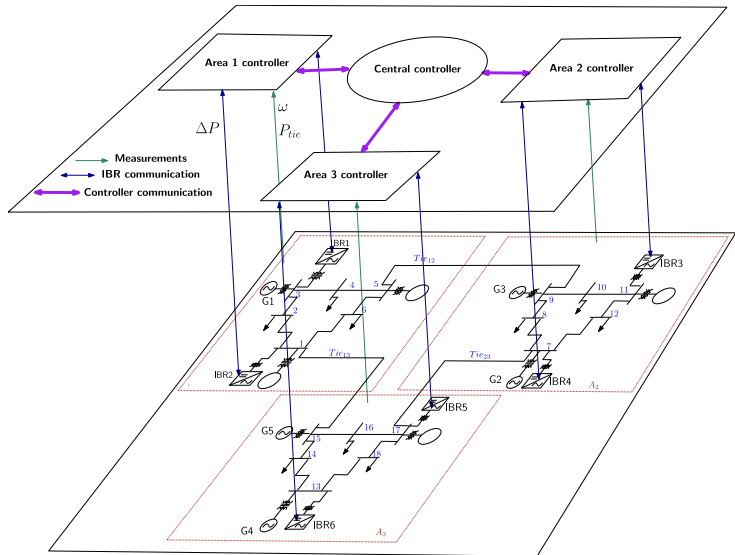
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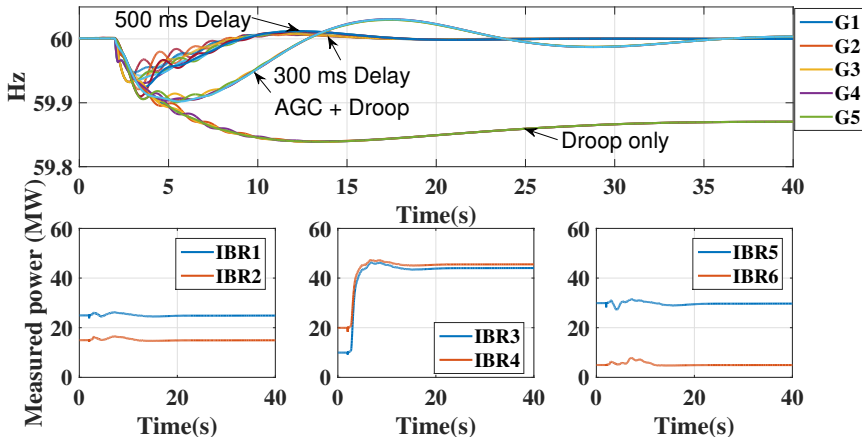
Case Study: Three-Area System

About 230MW per area



Scenario: 63 MW Disturbance, Area 2

- Design based on **lumped** generator + governor model

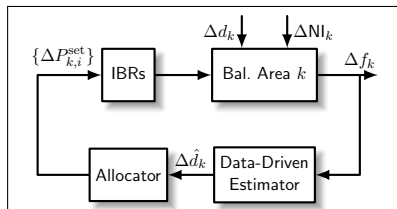


Localized Response in Area 2

Data-Driven Fast Frequency Control

E. Ekomwenrenren et al., "Data-Driven Fast Frequency Control ...," in IEEE TPWRS, 2024 (Hopefully!)

The *model-based* estimator can be replaced with a direct **data-driven estimator**



- 1 **Offline**: excite the area with IBRs and collect T samples of I/O data:

$$\Delta v_d = (\Delta v_d(1), \Delta v_d(2), \dots, \Delta v_d(T)), \quad v = \Delta P^{\text{set}} + \Delta NI$$
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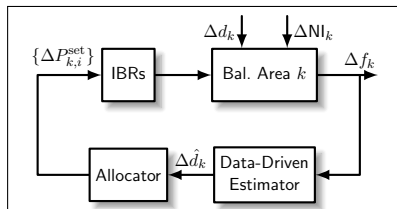
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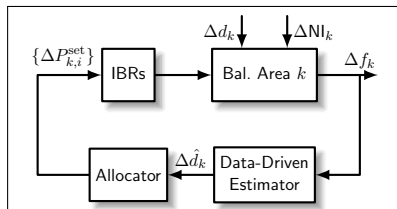
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- 3 **Online:** perform **data-driven simulation** to predict $\Delta f(t)$:

$$\underbrace{\begin{bmatrix} \mathcal{H}_{T_p+1}(\Delta v_d) \\ \mathcal{H}_{T_p+1}(\Delta y_d) \end{bmatrix}}_{\text{Hankel}} g \triangleq \begin{bmatrix} V_p \\ V \\ F_p \\ F \end{bmatrix} g = \begin{bmatrix} \Delta v_p + \Delta \hat{d}_p \\ \mathbf{0} \\ \Delta \hat{f}_p \\ \Delta \hat{f}(t) \end{bmatrix} \Rightarrow \Delta \hat{f}(t) = F \begin{bmatrix} V_p \\ V \\ F_p \end{bmatrix}^\dagger \begin{bmatrix} \Delta v_p + \hat{d}_p \\ \mathbf{0} \\ \Delta \hat{f}_p \end{bmatrix}$$

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$G(1) = \text{DC Gain}$ (computable directly from the above data)

This is a data-driven implementation of a disturbance estimator.
Optimization-based receding-horizon estimator also developed.

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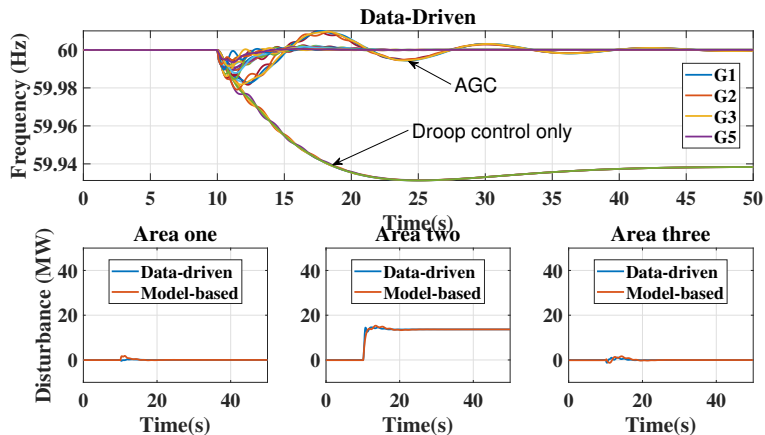
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Scenario: 60 MW Disturbance, Area 2

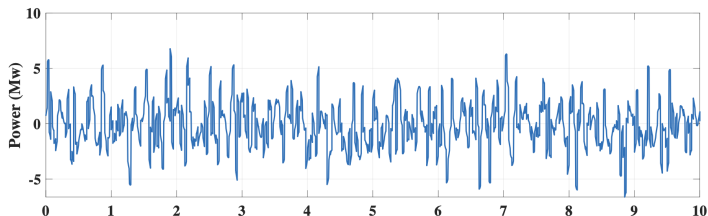


- Imbalance is **quickly localized and rejected** by controller
- Fast emergency control to enhance grid reliability

Comments on Data for Data-Driven Collection

- Probing power injection = harmonic + noise

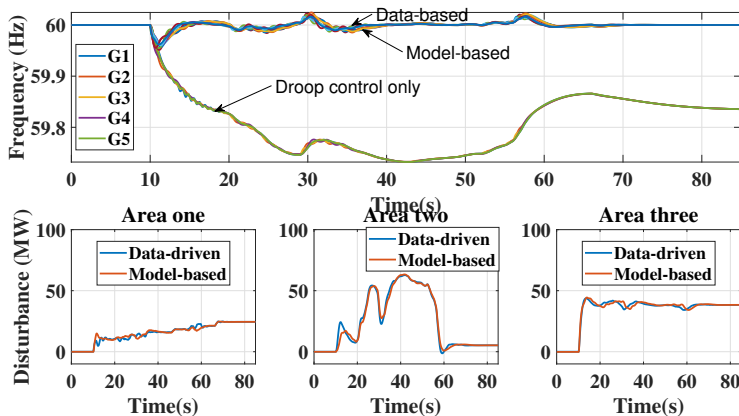
$$\Delta P_{ibr}(t) = \sin(12\pi t) + w(t)$$



- 10 samples/s for 10 seconds = **100 total data points**
- SVD truncation eliminates irrelevant dynamic modes
- Classical SysID (or equivalent) completely sufficient . . .

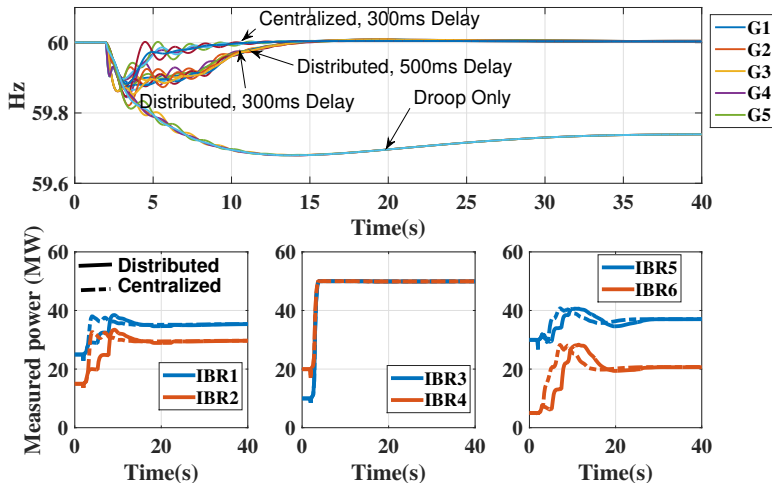
Scenario: Compensating for Renewables

- Uncontrolled wind and solar (≈ 300 MW) integrated into system
- Major unexpected decreases in RES across grid (≈ 125 MW total peak)

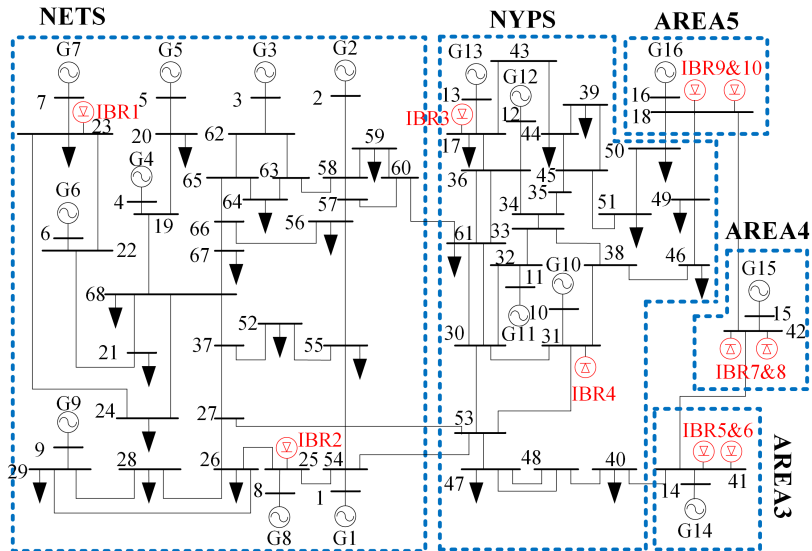


Scenario: 130MW Disturbance, Area 2

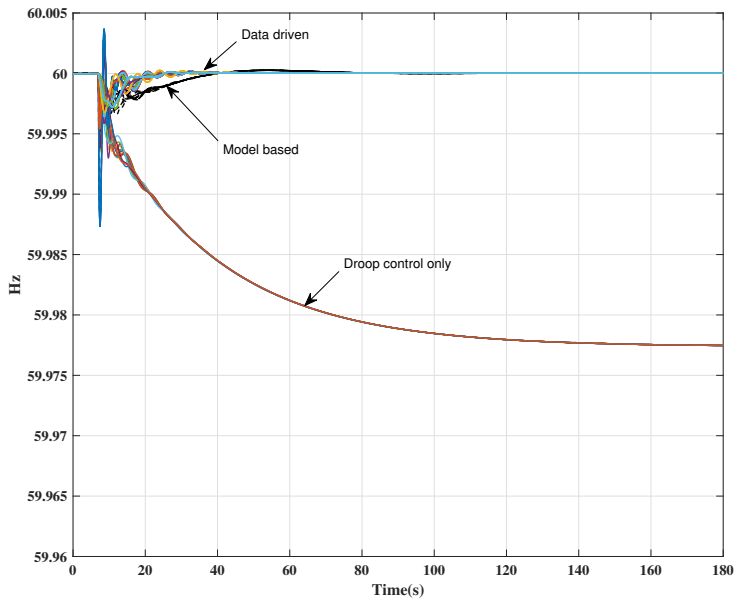
- Central controller kicks in when Area 2 runs out of supply



Five-Area 68 Bus Test System

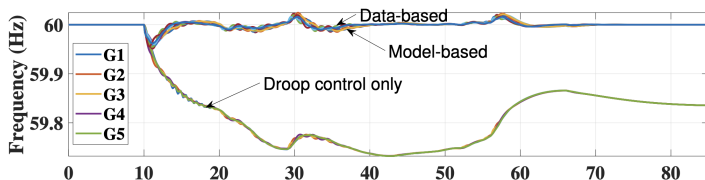


Scenario: 300MW Load Change in NYPS Area



Key Insights

Summary: You can significantly enhance frequency control **if** you have fast dispatchable reserves **and** a *bit* of advanced control.

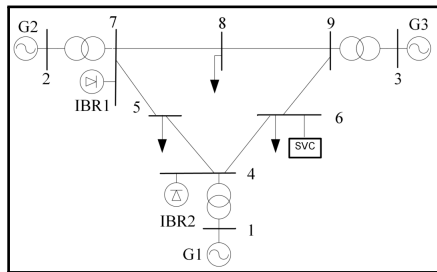


- Can provide contingency **resilience** for low-inertia systems
- As always, **beware of communication delays**

Challenge: where are these reserves going to come from?

Overview of Proposed Voltage Controller (One-Area)

Z. Tang et al. *Measurement-Based Fast Coordinated Voltage Control* ... in IEEE TPWRS, 2021.

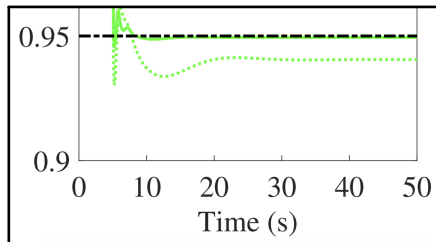
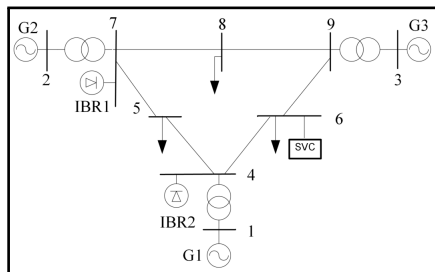


Control resources:

- SGs: $v_g^{\text{ref}} \longrightarrow q_g$
- SVCs: $v_s^{\text{ref}} \longrightarrow q_s$
- IBRs: $q_i^{\text{ref}} \longrightarrow q_i$

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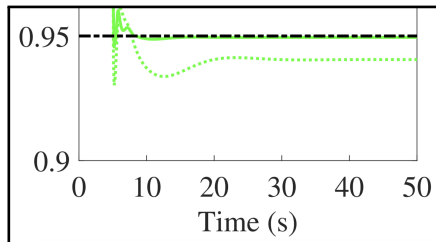
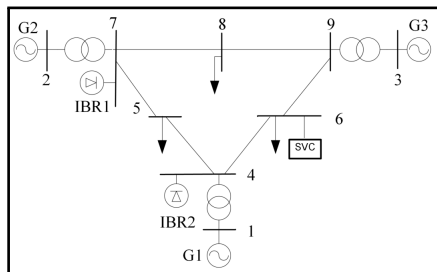


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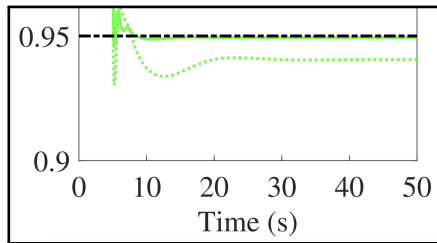
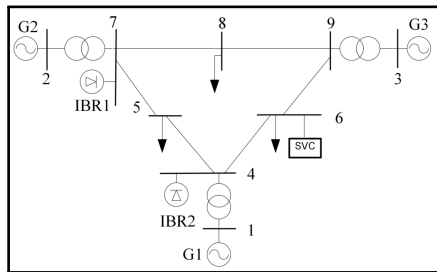


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- q = vector of power outputs

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Model:

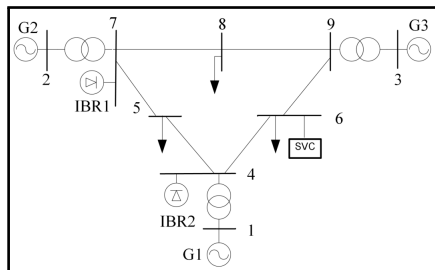
$$\dot{x} = f(x, u, w)$$
$$y = (v, q) = h(x, u, w)$$

$$\begin{array}{ll} \text{minimize} & J(q) \\ u \in \{\text{Limits}\} & \\ \text{subject to} & \text{voltage limits} \\ & \text{power limits} \end{array}$$

Steady-State Optimization Problem (One-Area)

Z. Tang et al. *Measurement-Based Fast Coordinated Voltage Control ...* in IEEE TPWRS, 2021.

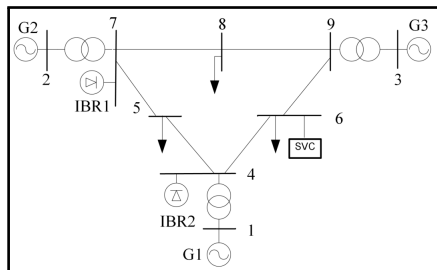
$$\begin{aligned} & \underset{v_g^{\text{ref}}, v_s^{\text{ref}}, q_i^{\text{ref}}}{\text{minimize}} && \text{Priority}(q_g, q_s, q_i) + \text{PenaltyFcn}(q_g, q_s, v) := F(u, y) \\ & \text{subject to} && y = (q_g, q_s, v) = \pi(v_g^{\text{ref}}, v_s^{\text{ref}}, q_i^{\text{ref}}, w) = \pi(u, w) \\ & && u = (v_g^{\text{ref}}, v_s^{\text{ref}}, q_i^{\text{ref}}) \in \mathcal{U} \end{aligned}$$



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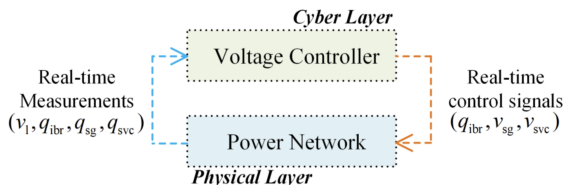


- vector y assumed to be **measurable** in real-time
- π = steady-state grid model
- **approximate sensitivities**
 $\Pi \approx \frac{\partial \pi}{\partial u}$ via load flow model

Feedback Implementation of Voltage Controller

Z. Tang et al. *Measurement-Based Fast Coordinated Voltage Control* ... in IEEE TPWRS, 2021.

$$u_{k+1} = \text{Proj}_{\mathcal{U}} \left\{ u_k - \alpha \left(\nabla_u F(u_k, y_k) + \Pi^T \nabla_y F(u_k, y_k) \right) \right\}$$



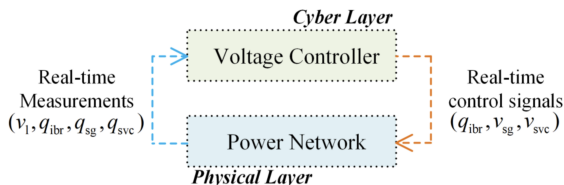
- Advantages:

- Optimizes system resources and maintains constraints
- Simple to implement and tune
- Integrates with legacy voltage control systems
- Comes with stability guarantees

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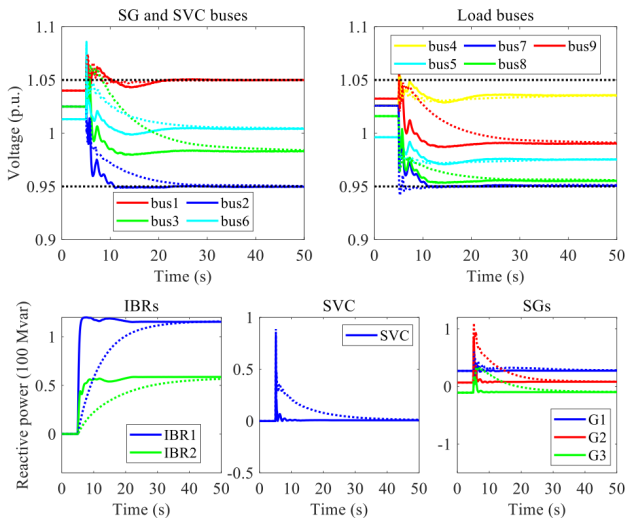
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Scenario: IBRs Providing Reactive Power Support

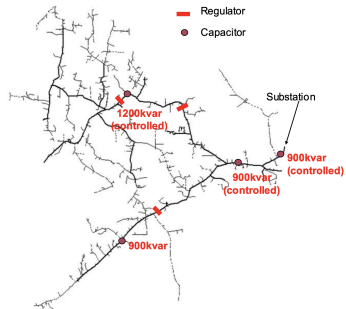
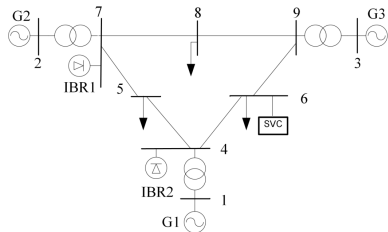
solid: with proposed controller

dotted: **ignore**



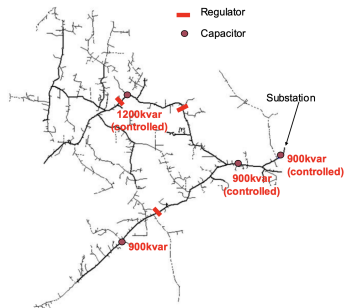
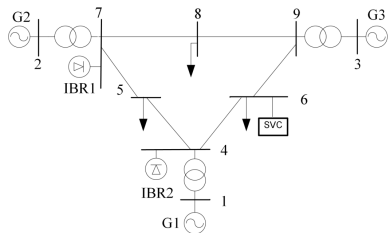
The Need for Transmission-Distribution Coordination

- Only very large storage and RES facilities are transmission-connected
- Most RES/DERs are connected at the **distribution level**



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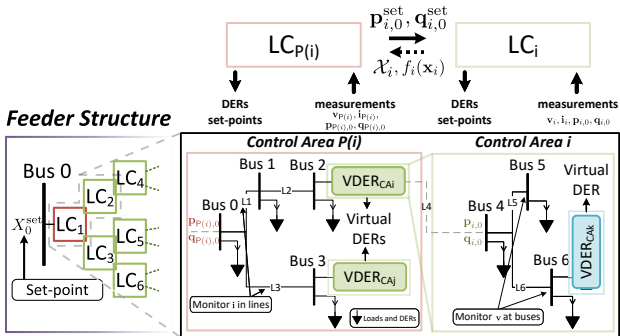
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Can we **hierarchically coordinate** resources in the distribution system to **collectively respond** like a fast transmission-connected resource?

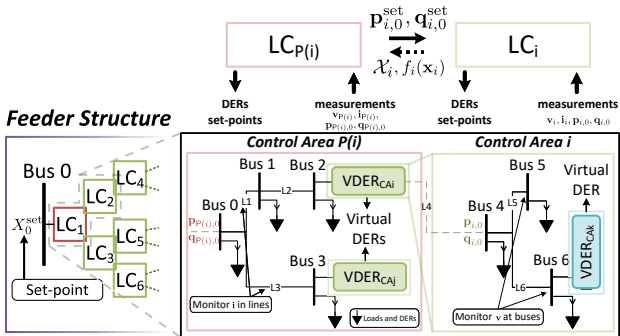
Multi-Area Hierarchical DN Control: Objectives

- (i) Respond **fast** to power change requests by TSO
- (ii) **Area-based** (e.g., aggregator) control using only local measurements
- (iii) Maintain voltage and current constraints in DN
- (iv) Grid and DER models kept **private** to each area controller
- (v) Design must be **agnostic** to specifics of DERs



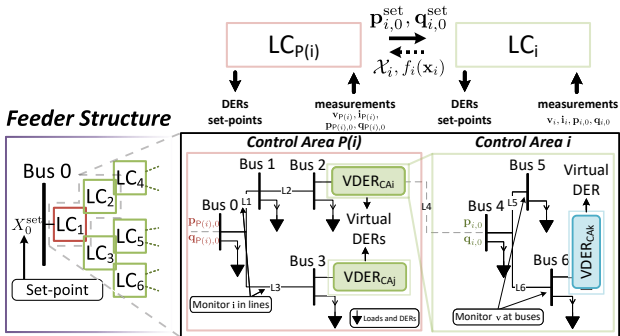
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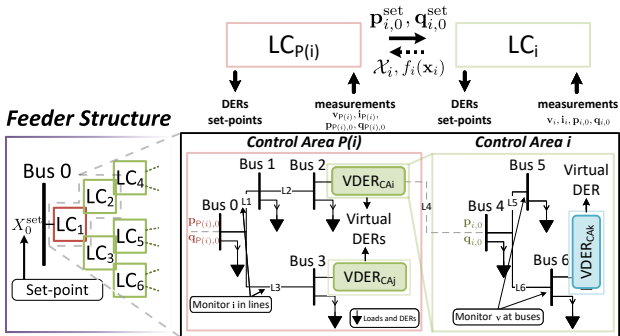
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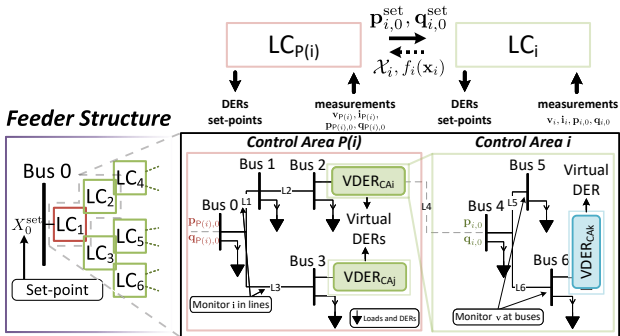
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Area Controller Design

Farhat et al. A Multi-Area Architecture for Real-Time Feedback-Optimization . . . , IEEE TSG, 2024 (Hopefully!)

Control Area i Design:

- $x_j = (p_j, q_j)$ are DER **set-points**
- *Child areas* $\mathcal{C}(i)$ abstracted as **virtual DERs**
- $f_{ij}(x_j) =$ control cost of DER j
- $\mathbf{p}_{i,0}, \mathbf{q}_{i,0} =$ power export to the *Parent Area* $\mathcal{P}(i)$

$$\underset{\mathbf{x}_i \in \mathcal{X}_i}{\text{minimize}} \quad \sum_{j \in \mathcal{D}_i} f_{ij}(x_j)$$

$$\text{subject to} \quad \mathbb{1}^\top \mathbf{p}_{i,0}(\mathbf{x}_i) = \mathbf{p}_{i,0}^{\text{set}}(\mathbf{x}_{\mathcal{P}(i)})$$

$$\mathbb{1}^\top \mathbf{q}_{i,0}(\mathbf{x}_i) = \mathbf{q}_{i,0}^{\text{set}}(\mathbf{x}_{\mathcal{P}(i)})$$

$$\underline{\mathbf{v}}_i \leq \mathbf{v}_i(\mathbf{x}_i) \leq \bar{\mathbf{v}}_i$$

$$\mathbf{i}_i(\mathbf{x}_i) \leq \bar{\mathbf{i}}_i$$

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Algorithm 1: LC Controller for i th CA

At each sampling time

[Step 1]: Receive set-points from LC of parent area $\mathcal{P}(i)$

$$\mathbf{p}_{i,0}^{\text{set}}(\mathbf{x}_{\mathcal{P}(i)}) = T_i^{\mathbf{p}} \mathbf{x}_{\mathcal{P}(i)}, \quad \mathbf{q}_{i,0}^{\text{set}}(\mathbf{x}_{\mathcal{P}(i)}) = T_i^{\mathbf{q}} \mathbf{x}_{\mathcal{P}(i)}$$

[Step 2]: Collect local measurements $\mathbf{p}_{i,0}, \mathbf{q}_{i,0}, \mathbf{v}_i, \mathbf{i}_i, \underline{\mathbf{x}}_i, \bar{\mathbf{x}}_i$

[Step 3]: LC performs the updates

$$\lambda_i^+ = \mathcal{P}_{\geq 0} \left(\lambda_i + \alpha_{\lambda_i} \left(\mathbb{1}^\top \mathbf{p}_{i,0} - \mathbf{p}_{i,0}^{\text{set}} - E_{i_p} - r_{\lambda_i} \lambda_i \right) \right)$$

$$\mu_i^+ = \mathcal{P}_{\geq 0} \left(\mu_i + \alpha_{\mu_i} \left(\mathbf{p}_{i,0}^{\text{set}} - \mathbb{1}^\top \mathbf{p}_{i,0} - E_{i_p} - r_{\mu_i} \mu_i \right) \right)$$

$$\eta_i^+ = \mathcal{P}_{\geq 0} \left(\eta_i + \alpha_{\eta_i} \left(\mathbb{1}^\top \mathbf{q}_{i,0} - \mathbf{q}_{i,0}^{\text{set}} - E_{i_q} - r_{\eta_i} \eta_i \right) \right)$$

$$\psi_i^+ = \mathcal{P}_{\geq 0} \left(\psi_i + \alpha_{\psi_i} \left(\mathbf{q}_{i,0}^{\text{set}} - \mathbb{1}^\top \mathbf{q}_{i,0} - E_{i_q} - r_{\psi_i} \psi_i \right) \right)$$

$$\gamma_i^+ = \mathcal{P}_{\geq 0} \left(\gamma_i + \alpha_{\gamma_i} \left(\mathbf{v}_i - \bar{\mathbf{v}}_i - r_{\gamma_i} \gamma_i \right) \right)$$

$$\nu_i^+ = \mathcal{P}_{\geq 0} \left(\nu_i + \alpha_{\nu_i} \left(\underline{\mathbf{v}}_i - \mathbf{v}_i - r_{\nu_i} \nu_i \right) \right)$$

$$\zeta_i^+ = \mathcal{P}_{\geq 0} \left(\zeta_i + \alpha_{\zeta_i} \left(\mathbf{i}_i - \bar{\mathbf{i}}_i - r_{\zeta_i} \zeta_i \right) \right)$$

[Step 4]: LC updates (V)DER set-points

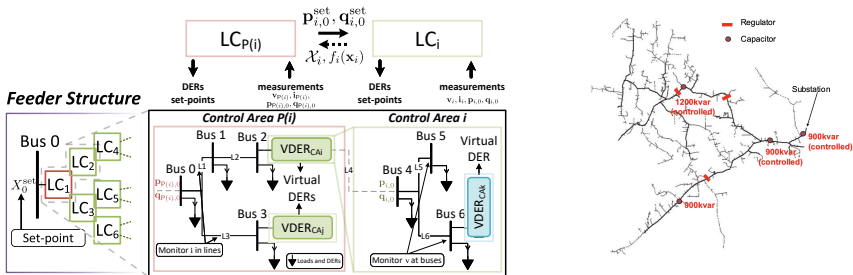
$$\mathbf{x}_i^+ = \arg \min_{\mathbf{x}_i \in \mathcal{X}_i} L_i^t(\mathbf{x}_i, \mathbf{d}_i^+; \mathbf{x}_{\mathcal{P}(i)})$$

[Step 5]: Transmit set-points to LCs of each child area

$$\mathbf{p}_{j,0}^{\text{set}}(\mathbf{x}_i^+) = T_j^{\mathbf{p}} \mathbf{x}_i^+, \quad \mathbf{q}_{j,0}^{\text{set}}(\mathbf{x}_i^+) = T_j^{\mathbf{q}} \mathbf{x}_i^+, \quad j \in \mathcal{C}(i).$$

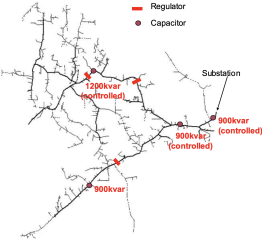
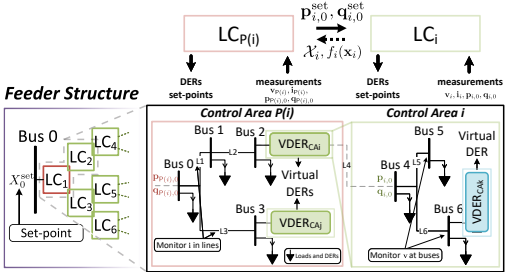
Design Features

- **Local measurements** used only by **local** controller (minimize delay)
- Local control requires only **local grid sensitivity model** (e.g., $p_{i,0} = \mathbf{A}_i \mathbf{x}_i$, etc.)
- Real-time feedback confers **robustness** to model uncertainty; stability guarantees
- Computationally simple, systematically tunable
- Scalable to **arbitrary numbers** of coordinated areas



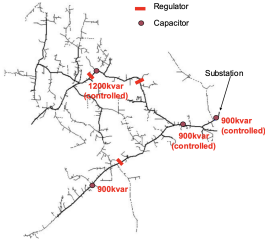
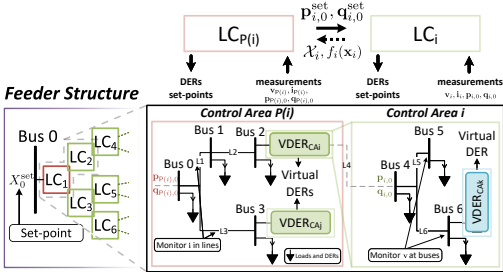
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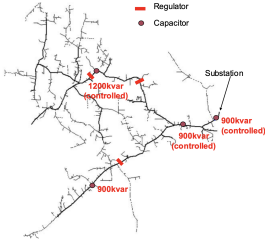
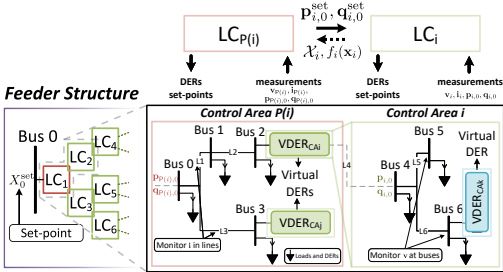
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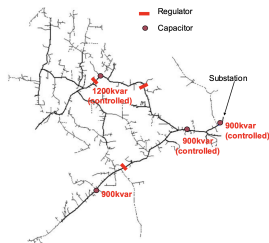
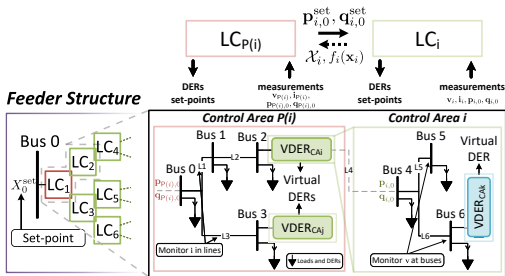
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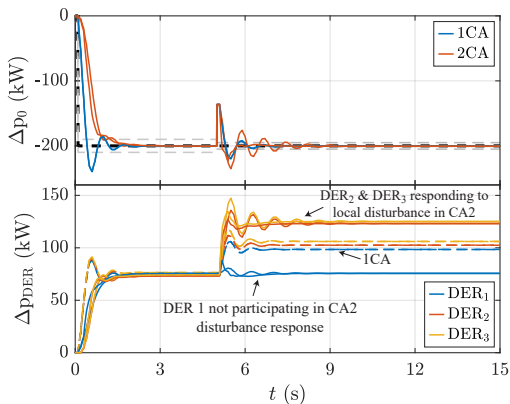
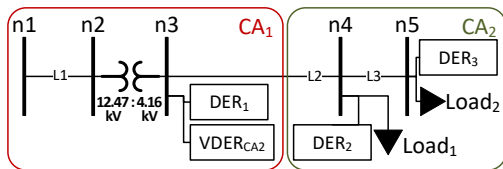


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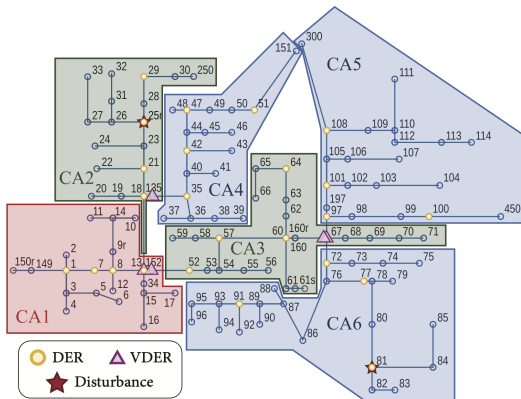
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Toy Example: Five-Bus Feeder, 200kW Request

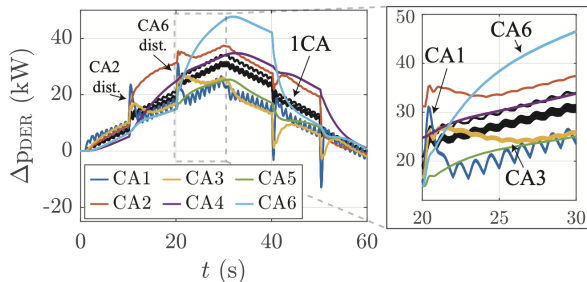
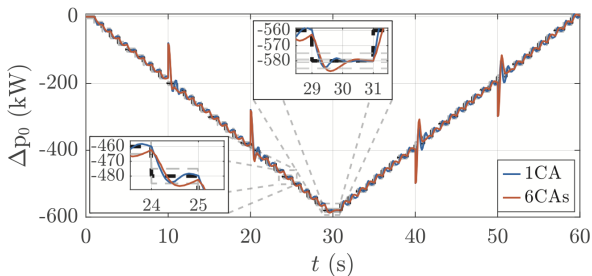


Example: 123 Bus Feeder

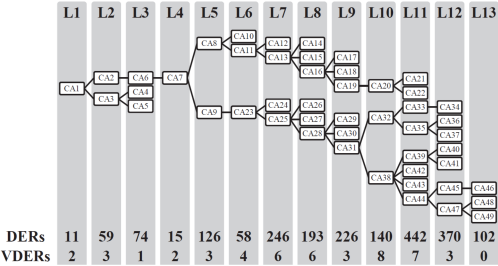
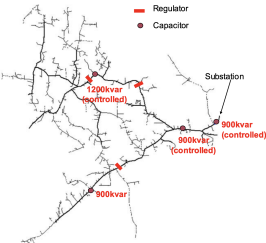


- 6 Control Areas
- 17 DERs
- Track **ramp signal** from TSO

Example: 123 Bus Feeder

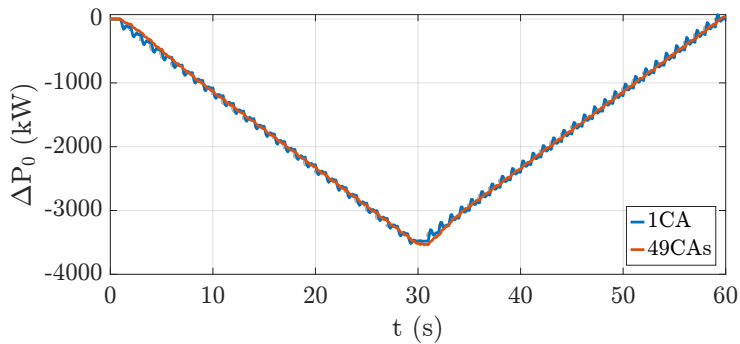


Example: 8500 Bus Feeder

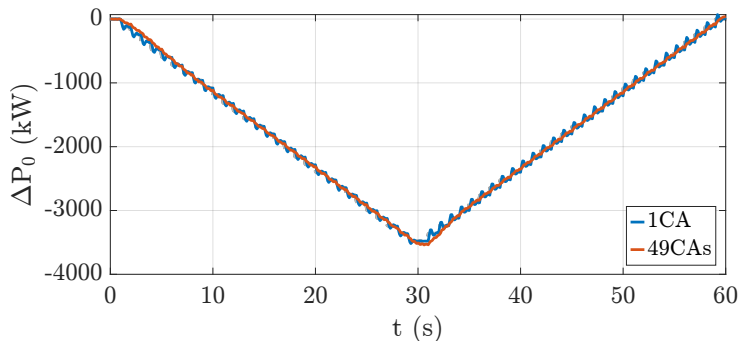


- 49 Control Areas
- 13 Nested Levels
- 2062 DERs (mix of 1 ϕ , 2 ϕ , and 3 ϕ -connected) with \approx 1s response time
- Track ramp signal from TSO

Example: 8500 Bus Feeder



Example: 8500 Bus Feeder



Our Next Goal: Demonstrate integration of this TN-DN coordination scheme with transmission-level fast frequency controller.

Conclusions

- Fast frequency and voltage control using TN-connected IBRs
- Fast, hierarchical, and scalable TN-DN coordination
- **Next:** Integration of controllers

Opportunities at $\{\text{control}\} \cap \{\text{energy systems}\} \cap \dots$

- Control architecture design
- Data-driven and learning-based control w/ guarantees ...

Parting thoughts:

- *Now is the moment for control to impact grid operations*
- Should control architectures mirror market architectures?
- Reliability/resilience must remain king

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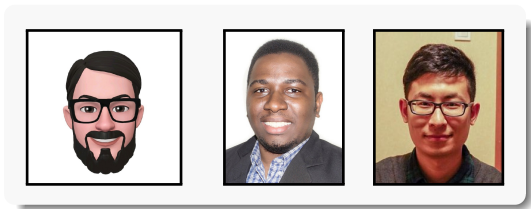
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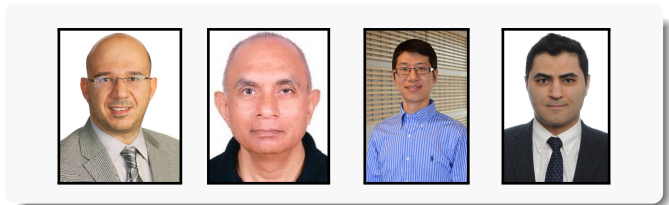
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Collaborators

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Questions



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appendix

A Problem of Scale

- In North America *balancing authorities* are the current “control areas”.

